Comparison of Nine Meteorological Drought Indices Over Middle Euphrates Region During Period from 1988 To 2017

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Abstract

The aim of this research is compare between nine drought indices and evaluate their performance with respect to predict and monitoring drought over Middle Euphrates region during period from 1988 to 2017. These indices are RDI, Normal SPI, Gamma SPI, Log SPI, CZI, MCZI, RAI, PN, and DI. Season and annual time scale were used to calculate all indices at Dewaniya, Hilla, Karbala, Najaf, and Semawa stations. The Pearson correlation coefficient between nine drought indices were analyzed. Annual and seasonal results illustrated that the maximum value of correlation between RDI and the other indices was noted with Gamma SPI and Log SPI at all stations. In annual time scale, the correlation coefficient reached to (0.99) at all stations except Hilla station, where it reached to (0.98), while in seasonal time scale the correlation coefficient reached to (0.98) at all stations. The RDI, Gamma SPI and Log SPI indices have similarity of classes and frequencies for drought. They also have similarity of frequencies for wet but there are minimum differences between wet classes compared to other indices. The RDI, Gamma SPI and Log SPI are good indices to predict and monitoring drought in study area in comparison to other indices which mentioned above.

Keywords: DI, Drought indices, Gamma SPI, Middle Euphrates Region, RDI

1. Introduction

Dry spell is ordinary wonder that results from proceeding with absences of rain over stretched out timeframe contrasted with some long haul typical conditions, prompting water needs for a few exercises or the natural division (Sammartin et al, 2018). Dry season varies from other ordinary perils since dry season develops step by step, making it difficult to pinpoint the start and end of an event. On an exceptionally essential dimension a dry season is a deficiency in the typical open water in a given hydrological system (Barker et al, 2016). Breaking down precipitation information is one of the strategies to examine dry spell, which is considered as a standout amongst the most widely recognized techniques (Najjar and Ramandi, 2015). UNDP (2008) characterizes dry spell as wonder that happens normally when precipitation is underneath normally recorded dimensions, causing genuine hydrological disturbances that contrarily impact on Earth asset creation frameworks (Babu, 2016). Usage of dry season files is important for watching and anticipating dry season. Additionally, these files empower to assess dry spell peril. Albeit none of these files is better than another, some capacity superior to anything others improve the situation a few applications and hydro-atmosphere conditions. The dry season checking framework is affected by an exact decision of lists for dry spell location, giving target depiction of dry spell conditions. In this way, it is basic the appropriateness of various dry season lists be evaluated and the best record be chosen (Eshghabad et al, 2014). In this exploration, nine meteorological dry spell lists were utilized, to be specific the RDI List, Typical SPI list, Log SPI record, Gamma SPI list, CZI list, MCZI file, RAI list, PN List and DI file. All these files were connected for a similar arrangement of meteorological information 1988–2017 and the fundamental time unit was season and yearly.

2. Materials and Methods

2.1. Area of study

The area of study is located in the Middle Euphrates Region. It is bounded by the coordinates (from 43°30’ E to 45°30’ E) longitude and (from 31°0’ N to 33°0’ N) latitude in zone 38N according to UTM projected coordinate system. It covers an area of 26611 Km² (figure 1). The climate of study area is arid to semi-arid with dry hot in summer and cool in winter. Rainfall in the area begins in October and ends in May after which it becomes scarce.

Fig. 1: Iraq map with a map represents the study area (Modified by authors based on Iraq administrative map scale 1:1000000, Ministry of water resources/General Directorate for Survey 2006)
2.2. Meteorological data

In this research, average rainfall and average temperature data were used to compute the drought indices. Monthly average rainfall, and monthly average temperature data were obtained from Iraqi Meteorological Organization and Seismology (IMOAS). Thirty years from 1988 to 2017 of data were obtained from five gauge stations over the study area and these stations are as illustrate in Table 1.

<table>
<thead>
<tr>
<th>Gauge</th>
<th>Name</th>
<th>E (Degree)</th>
<th>N (Degree)</th>
<th>Gauge Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Dewaniya</td>
<td>44.98</td>
<td>31.98</td>
<td>Surface Station</td>
</tr>
<tr>
<td>2</td>
<td>Hilla</td>
<td>44.43</td>
<td>32.48</td>
<td>Surface Station</td>
</tr>
<tr>
<td>3</td>
<td>Karbala</td>
<td>44.01</td>
<td>32.61</td>
<td>Surface Station</td>
</tr>
<tr>
<td>4</td>
<td>Najaf</td>
<td>44.31</td>
<td>31.98</td>
<td>Surface Station</td>
</tr>
<tr>
<td>5</td>
<td>Semawa</td>
<td>45.26</td>
<td>31.3</td>
<td>Surface Station</td>
</tr>
</tbody>
</table>

2.3. Meteorological drought indices

In this research, nine drought indices were used, the details of these indices is described below:

2.3.1. Standardized Precipitation Index (SPI)

SPI is index for monitoring drought created by McKee et al. in 1993 using fitting a gamma distribution for station frequency distribution of rain total. McKee et al developed this index and computed it according to periods such as 3, 6, 12, 24, 36 and 48 months. These periods reflect the effect of wetness and dryness on the availability of water resources. Short period precipitation anomalies effect soil wetness and long period precipitation anomalies effect on water resources (Khan and Gadiwala, 2013). Positive values of this index indicate more precipitation than expect for a given period can be computed as follows (Kumar et al, 2016):

\[ G(x) = \frac{1}{\beta \Gamma(\alpha)} x^{\alpha - 1} e^{-x/\beta} \quad \text{for } x, \alpha, \beta > 0 \]  

Where: \( \alpha \) and \( \beta \) are the shape parameters, \( X \) is the precipitation amount in mm and \( \Gamma(\alpha) \) is the Gamma function of \( \alpha \).

\[ \Gamma(\alpha) = \int_0^\infty y^{\alpha-1} e^{-y} dy \]  

\[ \alpha \text{ and } \beta \text{ parameters are computed as follow:} \]

\[ \alpha = \frac{1}{4 \times \chi^2} \int_b^\infty y^{\alpha-1} e^{-y/\chi} \text{ d}y \]  

\[ \chi = \frac{\chi}{\alpha} \]  

\[ A = \ln(x) - \frac{\ln(x)}{n} \]

Where, \( x \) is average rainfall in mm of all data of same event, \( n \) is number of precipitation data. After calculating values of \( \alpha \), \( \beta \), and \( A \), the cumulative probability of the observed precipitation for a given period can be computed as follows:

\[ G(x) = \frac{1}{\beta \Gamma(\alpha)} \int_b^x y^{\alpha-1} e^{-y/\chi} \text{ d}y \]  

\[ H(x) = Q + (1-Q) G(x) \]

(Kumar et al, 2016):

\[ SPI = -\left( t - \frac{2.515517 + 0.802853 \times t + 0.010328 \times t^2}{1 + 1.432788 \times t + 0.189369 \times t^2 + 0.001308 \times t^3} \right) \]  

(8)

If \( 0 < H(x) \leq 0.5 \)

When \( t = \frac{\ln(1/1-H(x)^2)}{\sqrt{\ln(1/0.5)}} \)  

(9)

\[ SPI = + \left( t - \frac{2.515517 + 0.802853 \times t + 0.010328 \times t^2}{1 + 1.432788 \times t + 0.189369 \times t^2 + 0.001308 \times t^3} \right) \]  

(10)

If \( 0.5 < H(x) \leq 1 \)

When \( t = \frac{\ln(1/1-H(x)^2)}{\sqrt{\ln(1/0.5)}} \)  

(11)

(Yacoub and Tayfur, 2017).

\[ SPI = \frac{\ln(x) - \mu}{\sigma} \]  

(12)

It may be sometimes more effective, at the arithmetic level, to standardize the data directly from a fitted natural distribution where possible. Normal SPI is calculated as follow:

\[ SPI = \frac{x - \mu}{\sigma} \]  

(13)

Where, \( x \) is precipitation, \( \mu \) and \( \sigma \) are the average and standard deviation of precipitation, respectively. The categorization of drought based on three types of SPI which mentioned above are given in Table 2 (Yacoub and Tayfur, 2017).

2.3.2. Reconnaissance Drought Index (RDI)

This index is depends on the proportion between two accumulated amounts of precipitation and potential evapotranspiration. Utilization of ETo in the detection of drought has been useful in development of this index. The first step to compute this index is compute \( o \) and then computed it. Where, \( o \) is computed as following.

\[ o = \frac{\sum_{i=1}^{12} Rij}{\sum_{i=1}^{12} Etoij} \]  

(14)

Where: \( Rij \) and \( Etoij \) are precipitation and potential evapotranspiration of the jth month of the ith year.

\[ RDIStk = \frac{y_k - A(y_k)}{\sigma y_k} \]  

(15)

Where, \( y_k \) is the ln (\( o \)), \( A(y_k) \) is the average and \( \sigma y_k \) is the standardized deviation. The classes of RDI index were classified as shown in table 2 (Shah et al, 2013). In this research ETo was estimated using the Thornthwait method. The estimation of ETo was computed according to Thornthwaite (1948) by the equation (AI-Enzey, 2012):

\[ ETo = 16 \frac{41 \chi}{360} (10 \ln(f))^h \text{ mm/month} \]  

(16)

\[ J = \sum_{i=1}^{12} i \]  

(17)

\[ i = \lfloor tr/5 \rfloor \]  

(18)

\[ k = (675 \times 0.000000001) J^3 - (771 \times 0.000000001) J^2 + (179 \times 0.00000001) J + 0.492 \]  

(19)

Where:

\[ ETo = \text{Potential evapotranspiration for each month (mm / month)} \]  

\[ t = \text{Mean monthly temperature (°C)} \]
\( n = \) Number of month measurement  
\( J = \) Annual heat index (°C)  
\( i = \) monthly temperature parameter (°C)  
\( D: \) Number of the days a month.  
\( T: \) Average number of sunshine hours

### 2.3.3. China-Z index (CZI), modified CZI (MCZI)

The CZI is based on the Wilson Hilferty cube root conversion. The index is calculated as:

\[
CZI_i = \frac{6}{C} \left( \frac{2}{C} Q_i + 1 \right)^{1/3} - \frac{6}{C} + \frac{C}{6}
\]

\[
C = \frac{\sum (x_i - \bar{x})^2}{n \sigma^2}
\]

\[
Q_i = \left( \frac{x_i - \bar{x}}{\sigma} \right)
\]

Where \( i \) is the current month, \( C \) is skewness coefficient, \( n \) is the total number data, \( Q_i \) is standard variate, \( x_i \) is rainfall of \( i \) month, and \( \bar{x} \) is average of precipitation. To calculate the MCZI, the median of precipitation is utilized rather than the mean of precipitation in the calculation of the CZI (Morid et al, 2006). The classes of CZI and MCZI indices were classified as shown in table 2 (Soleimani et al, 2015).

### 2.3.4. Rainfall anomaly index (RAI)

This index was presented by Van Rooy (1965). It depends on the computation of the rainfall in comparison to accidental numbers from -3 to +3. In this index, the data is arranged in ascending manner from the highest to the lowest value, then by computing the mean of the ten highest and the ten lowest values of rainfall during the statistical period, the drought is computed according to the following equations:

\[
RAI = \frac{(R - \bar{R})}{(M - \bar{R})}, \quad \text{if } R > \bar{R}
\]

\[
RAI = \frac{(R - \bar{R})}{(X - \bar{R})}, \quad \text{if } R < \bar{R}
\]

Where: \( X \) is the mean of the ten lowest values of rainfall, \( M \) is the mean of the ten highest values of rainfall, \( \bar{R} \) is the long term mean rainfall, and \( \bar{R} \) is the rainfall value (Javan et al, 2016). The classes of this index are illustrated in Table 2 (Sammartin et al, 2018).

### 2.3.5. Percent of Normal precipitation Index (PN)

Alami et al, 2017 It is computed by the following relation:

\[
PN = \frac{\pi}{\bar{\pi}} \times 100
\]

Where: \( \pi \) is the normalized amount of precipitation of the current annual, \( \bar{\pi} \) is the mean of rainfall in timeframe for each station (Mokarram and Mahmoodi, 2015). The PN values are classified as shown in Table 2 (Alami et al, 2017).

### 2.3.6. Deciles Index (DI)

This index, basically designed by Gibbs and Maher 1967. It depends on ranged rainfall data from biggest to littlest in long term record to build cumulative distribution and then this distribution is divided into ten deciles. Any rainfall value can be compared with these deciles. Equation for compute this index is:

\[
P_I = \frac{i}{n+1} \times 100
\]

Where, \( pi \) is probability of rain in number \( ith \), \( n \) is number of rainfall data. Classes of this index are illustrated in Table 2 (Nohegar et al, 2015).

The values range of RAI, PN, and DI are not similar to values range of SPI, RDI, CZI and MCZI indices. Therefore, rank values were used to make them comparable with the SPI, RDI, CZI and MCZI indices.

### 3. Results and Discussion

This research focused on comparison between known nine meteorological drought indices (RDI, Gamma SPI, Log SPI, Normal SPI, CZI, MCZI, RAI, PN, DI) over five stations of middle Euphrates region during period 1988 to 2017. These stations are Deywaniya, Hilla, Karbala, Najaf, and Semawa. Middle Euphrates region is famous with agricultural, therefore seasonal and annual time scale were used to calculate drought indices which mentioned above. In seasonal time scale, only rainy seasons such as winter, spring, and autumn seasons were used to calculate all indices in all stations.

#### Table 2: The categorization of drought indices

<table>
<thead>
<tr>
<th>Rank</th>
<th>Drought classes</th>
<th>SPI,DL,CZI, And MCZI</th>
<th>RAI</th>
<th>PN %</th>
<th>DI %</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>Extremely wet</td>
<td>&gt;2</td>
<td>&gt;3</td>
<td>&gt;180</td>
<td>&gt;90</td>
</tr>
<tr>
<td>2</td>
<td>Severely wet</td>
<td>1.5 to 1.99</td>
<td>2</td>
<td>161</td>
<td>80</td>
</tr>
<tr>
<td>1</td>
<td>Moderately wet</td>
<td>1 to 1.49</td>
<td>1.99</td>
<td>121</td>
<td>70</td>
</tr>
<tr>
<td>0</td>
<td>Near normal</td>
<td>-0.99 to 0.99</td>
<td>0.99</td>
<td>81</td>
<td>30</td>
</tr>
<tr>
<td>-1</td>
<td>Moderately drought</td>
<td>-1 to -1.49</td>
<td>-1</td>
<td>41</td>
<td>20</td>
</tr>
<tr>
<td>-2</td>
<td>Severely drought</td>
<td>-1.5 to -1.99</td>
<td>-2</td>
<td>21</td>
<td>10</td>
</tr>
<tr>
<td>-3</td>
<td>Extremely drought</td>
<td>&lt;= -2</td>
<td>&lt;= 3</td>
<td>&lt;=20</td>
<td>&lt;=10</td>
</tr>
</tbody>
</table>

The Pearson’s correlation coefficient matrix was used for the nine drought indices for each meteorological station. The RDI index was considered a reference for comparison with the other indices which mentioned above because it based on precipitation and potential evapotranspiration factor compared to other indices that relied on rainfall only. The annual and seasonal results illustrated that the maximum value of correlation between RDI index and the other indices was noted with Gamma SPI and Log SPI indices at all stations. In annual time scale, the correlation coefficient reached to (0.99) at all stations except Hilla station, where it reached to (0.98). However, in seasonal time scale the correlation coefficient reached to (0.98) at all stations as shown in tables from 3 to 6. On the other hand, the RDI, Gamma SPI and Log SPI indices have similarity of classes and frequencies for drought and it have similarity of frequencies for wet but there are minimum differences between wet classes compared to the other indices. The RAI, PN, and DI indices have higher frequencies for drought and wet classes compared with the other indices as shown in figures from 2 to 21. This meaning the RDI, Gamma SPI and Log SPI were good indices to predict and monitoring drought in study area compared with the other indices which mentioned above. On other hand the results of RDI, Gamma SPI, and Log SPI illustrated that the study area was suffered from periods of drought during period 1988 to 2017 according to each station in it whether annual or seasonal as shown in figures from 2 to 17.
**Table 3** The correlation coefficient between RDI index and the other indices (Annual time scale)

<table>
<thead>
<tr>
<th>Indices</th>
<th>Dewaniya Station</th>
<th>Hilla Station</th>
<th>Karbala Station</th>
<th>Najaf Station</th>
<th>Semawa Station</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gamma SPI</td>
<td>0.99</td>
<td>0.98</td>
<td>0.99</td>
<td>0.99</td>
<td>0.99</td>
</tr>
<tr>
<td>Log SPI</td>
<td>0.99</td>
<td>0.98</td>
<td>0.99</td>
<td>0.99</td>
<td>0.99</td>
</tr>
<tr>
<td>Normal SPI</td>
<td>0.91</td>
<td>0.92</td>
<td>0.96</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>CZI</td>
<td>0.96</td>
<td>0.97</td>
<td>0.97</td>
<td>0.94</td>
<td>0.91</td>
</tr>
<tr>
<td>MCZI</td>
<td>0.96</td>
<td>0.94</td>
<td>0.97</td>
<td>0.94</td>
<td>0.91</td>
</tr>
<tr>
<td>RAI</td>
<td>0.84</td>
<td>0.85</td>
<td>0.85</td>
<td>0.83</td>
<td>0.82</td>
</tr>
<tr>
<td>PN</td>
<td>0.89</td>
<td>0.83</td>
<td>0.90</td>
<td>0.86</td>
<td>0.81</td>
</tr>
<tr>
<td>DI</td>
<td>0.71</td>
<td>0.81</td>
<td>0.83</td>
<td>0.83</td>
<td>0.80</td>
</tr>
</tbody>
</table>

**Table 4** The correlation coefficient between RDI index and the other indices (Winter time scale)

<table>
<thead>
<tr>
<th>Indices</th>
<th>Dewaniya Station</th>
<th>Hilla Station</th>
<th>Karbala Station</th>
<th>Najaf Station</th>
<th>Semawa Station</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gamma SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Log SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Normal SPI</td>
<td>0.97</td>
<td>0.93</td>
<td>0.94</td>
<td>0.96</td>
<td>0.97</td>
</tr>
<tr>
<td>CZI</td>
<td>0.97</td>
<td>0.97</td>
<td>0.97</td>
<td>0.97</td>
<td>0.95</td>
</tr>
<tr>
<td>MCZI</td>
<td>0.97</td>
<td>0.96</td>
<td>0.96</td>
<td>0.95</td>
<td>0.89</td>
</tr>
<tr>
<td>RAI</td>
<td>0.66</td>
<td>0.74</td>
<td>0.78</td>
<td>0.67</td>
<td>0.70</td>
</tr>
<tr>
<td>PN</td>
<td>0.80</td>
<td>0.81</td>
<td>0.87</td>
<td>0.85</td>
<td>0.75</td>
</tr>
<tr>
<td>DI</td>
<td>0.65</td>
<td>0.70</td>
<td>0.78</td>
<td>0.65</td>
<td>0.59</td>
</tr>
</tbody>
</table>

**Table 5** The correlation coefficient between RDI index and the other indices (Spring time scale)

<table>
<thead>
<tr>
<th>Indices</th>
<th>Dewaniya Station</th>
<th>Hilla Station</th>
<th>Karbala Station</th>
<th>Najaf Station</th>
<th>Semawa Station</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gamma SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Log SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Normal SPI</td>
<td>0.95</td>
<td>0.87</td>
<td>0.80</td>
<td>0.94</td>
<td>0.96</td>
</tr>
<tr>
<td>CZI</td>
<td>0.97</td>
<td>0.96</td>
<td>0.95</td>
<td>0.97</td>
<td>0.94</td>
</tr>
<tr>
<td>MCZI</td>
<td>0.92</td>
<td>0.96</td>
<td>0.88</td>
<td>0.95</td>
<td>0.95</td>
</tr>
<tr>
<td>RAI</td>
<td>0.83</td>
<td>0.85</td>
<td>0.84</td>
<td>0.77</td>
<td>0.78</td>
</tr>
<tr>
<td>PN</td>
<td>0.87</td>
<td>0.83</td>
<td>0.84</td>
<td>0.83</td>
<td>0.78</td>
</tr>
<tr>
<td>DI</td>
<td>0.78</td>
<td>0.80</td>
<td>0.76</td>
<td>0.74</td>
<td>0.68</td>
</tr>
</tbody>
</table>

**Table 6** The correlation coefficient between RDI index and the other indices (Autumn time scale)

<table>
<thead>
<tr>
<th>Indices</th>
<th>Dewaniya Station</th>
<th>Hilla Station</th>
<th>Karbala Station</th>
<th>Najaf Station</th>
<th>Semawa Station</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gamma SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Log SPI</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
<td>0.98</td>
</tr>
<tr>
<td>Normal SPI</td>
<td>0.91</td>
<td>0.95</td>
<td>0.95</td>
<td>0.92</td>
<td>0.92</td>
</tr>
<tr>
<td>CZI</td>
<td>0.96</td>
<td>0.88</td>
<td>0.93</td>
<td>0.95</td>
<td>0.97</td>
</tr>
<tr>
<td>MCZI</td>
<td>0.90</td>
<td>0.83</td>
<td>0.93</td>
<td>0.95</td>
<td>0.89</td>
</tr>
<tr>
<td>RAI</td>
<td>0.84</td>
<td>0.79</td>
<td>0.77</td>
<td>0.87</td>
<td>0.78</td>
</tr>
<tr>
<td>PN</td>
<td>0.86</td>
<td>0.77</td>
<td>0.81</td>
<td>0.84</td>
<td>0.76</td>
</tr>
<tr>
<td>DI</td>
<td>0.84</td>
<td>0.75</td>
<td>0.77</td>
<td>0.76</td>
<td>0.77</td>
</tr>
</tbody>
</table>
4. Conclusion

1. Gamm SPI and Log SPI indices recorded high values of correlation with RDI index compared with the other indices.
2. The RDI, Gamma SPI and Log SPI indices have similarity of classes and frequencies for drought. They also have similarity of frequencies for wet but there are minimum differences between wet classes.
3. The RAI, PN, and DI indices have higher frequencies for drought and wet classes compared to other indices.
4. The RDI, Gamma SPI and Log SPI indices are good indices to predict and monitoring drought in study area.
5. Normal SPI, CZI, MCZI, RAI, PN, and DI indices are unsuitable to predict and monitoring drought in study area.

References


