# An algorithm to Convert the Gestures of Numbers of Four languages into Voice 

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#### Abstract

Gestures are one of the best ways of communication between dumbs people they can speak and other people they can speak using the expression of signs language. It is good to communicate between the dumb and other people by convert their signals into voices to be easy communicate with other people they can speak and hear voices. In this paper, a new algorithm proposed for recognizing hand gestures of numbers ( $0-10$ ) to four languages (English, Arabic, Chinese and Persian languages) depending on dumbs signs and convert the signs into voices corresponding to signs numbers of each language. The proposed algorithm, firstly uses video for gesture of the dumb to three languages then converts these videos into frames (images), secondly preprocessing step to removing the noises, resizing the images and increasing the contrast, the third step is extraction features step to calculating the distance of clustering algorithms such as Bayesian, C 4.5 , k-mean, k- medoid and artificial neural network. Eighteen features are calculated; eight features from Euclidean distance, eight features from slop, Area, and perimeter. The results in the training stage were; Bayesian gave $100 \%$ accuracy, C4.5 gave $100 \%$ accuracy, k-mean gave $100 \%$ accuracy k-medoid gave $100 \%$ accuracy and artificial neural network gave $95 \%$ accuracy. While in the testing stage classifiers are; Euclidian Distance, Modify Standardize Euclidian Distance and Correlation to calculating the difference between the features stored from training stage with new tested features and the results show that Euclidian Distance gave $100 \%$ accuracy, modified Standardize Euclidian Distance gave $100 \%$ accuracy and Correlation gave $100 \%$ accuracy. The database is created in our laboratory (six videos with 324 frames).


Keywords: Gestures, Feature Extraction, Bayesian, C4.5, K-Mean, K-Medoid, ANN, Numbers, Clustering.

## 1. Introduction

Communication is the way of people for expression Their ideas, thoughts, opinions or information between the people by writing, speaking, or signs. The dealing with people may be oral expression between ordinary people, while the dumbs people can't speak with ordinary people they can use signals to deal with the ordinary people [1].
Communication between people can be though the language to make them understand each other, but different languages may cause misunderstand the other people whom not native language such as Chinese language different from Arabic language, this problem may be solving by using translators for all languages, the dumb people have problem to communicate with normal people.
The gesture is a kind of nonverbal communication with a part of body such as hand or two hands signs for numbers, which used together with verbal communication. Same of people able to speaking and writing, but the others (dumb) could not only the can used gestures to deal with others and the gesture may change from person to another person, even the same person may change his gesture in some cases [2].
Dumb people use signs to express their ideas. Gesture language is different from country to another with its special vocabulary and grammarian. In fact, gesture language may be varied in the same country from place to another place as Languages spoken [3] so we used four languages (English, Arabic, Chinese and Persian languages). The gesture is the action of any part of hand or two hands motion [4].

There are many methods for recognizing the gesture; such as Bayesian, C4.5, k-mean, k- medoid and artificial neural network which based on special gloves. This method uses video and converts the video into frames to identify the pattern they know the hand gestures [5].
Recognizing of gesture language at present done by the token gesture to four languages (English, Arabic, Chinese and Persian languages) using video camera such as a professional camera, mobile camera, tablet camera, special camera, or laptop camera [6] then convert the video into images and also need to extracting the features of images at last classify each number to four languages (English, Arabic, Chinese and Persian languages) into corresponding voices, this paper focuses on how the gesture numbers of four languages (English, Arabic, Chinese and Persian languages) are translate into voices to make the dumb people communicate with other people through voices. The four languages (English, Arabic, Chinese and Persian languages) numbers gestures are shown in Figure 1.

## 2. Clustering algorithms and recognition

There are many algorithms used in this paper for recognition such as; Bayesian, C4.5, K-mean, K- Medoid algorithms and ANN. Which used for build database in training stage to compare the new images by the database stored from a training stage.

## 3. Proposed Algorithm

The proposed algorithm consists of two stages; training stage and testing stage, where the training stage contain five steps (images acquisition, pre-processing step, extraction of features, recognition
and store the database) while the testing stage contains the same steps from 1-4 and then compare the features extracted from new image with features in database as shown in Figure2 we had published paper related to this work but in fewer details and one language.


Figure 1.: Gestures of Arabic, Chinese, Persian and English Numbers


Figure 2: proposed algorithm

### 3.1 Dataset Acquisition

The database is created by using special cameras in the laboratory, where all images must have the same environments, the background of images have black colour and fix the position of the camera to be easy to remove the background and keep the signal only In this paper there are eleven numbers of English, Arabic, Chinese and Persian ( $0,1,2,3,4,5,6,7,8,9,10$ ) from different persons, where these images will be templates for database. The images size ( $640 * 480$ pixels) with JPEG formats.

### 3.2 Pre-Processing

The Pre-processing done by algrothim. 1 the following steps as shown in Figure 3:

## Algorithm 1

Input: image or frame from video.
Output: enhanced image.

1. Convert the video into images (frames).
2. Convert the image into gray scale format and resize image into $300 * 100$ pixel.
3. Convert image into a binary image
4. Apply morphological operations to de-noise from binary image.
5. End.

Figure 3: preprocessing steps for four languages

### 3.3 Segmentation

The Segmentation can be done by algorithm. 2 as shown in Figure 4.

## Algorithm 2

Input: enhanced image.
Output: binary image contains object (hand) only.

1. Create a mask from resulted image contains two values (1 and 0 ), 0 's for the hand background and 1 's for the hand sign part.
2. Multiply the resulted image from algrothm. 1 by the mask.
3. Using equation (1) [8], to calculate the rotation angle of resulted image and rotate image by using equation (2) [9].


$$
\begin{equation*}
\theta=\tan ^{-1}\left(\frac{s_{1}-s_{2}}{1+s_{1} * s_{21}}\right) . \tag{1}
\end{equation*}
$$

where: $s_{1}$ is the slope between A and B points is the $s_{2}$ slope between B and C points .
$\hat{z}=z * \cos (\theta)-w * \sin (\theta)\}$
$\widehat{w}=z * \sin (\theta)-w * \cos (\theta)\}$
4. Create a new mask from rotated image contains two values (1 and 0) 0 's for hand background and 1 's for the hand sign part.
5. Multiply the resulted image from step 3 by a new mask and convert the image into a binary image.
6. End

c)

English


Figure 4: segment steps for four languages

### 3.4 Feature Extraction

In this paper, we used the geometric features where there are 18 geometrics features extracted from each input image, divided into (eight-features of distance between the eight points within the centre of hand by using equation (3)[7]), (eight-features of slop between the eight points within the centre of hand by using equation (4)[8]), one- feature of area by using equation (6)[9] and last one-feature of perimeter (7)[10]. Also we need to find the centre of hand depending on equation (5)[11].
$D E_{z o}=\sqrt{\sum_{i=1}^{n}\left(x_{z i}-x_{o i}\right)^{2}}$
Where:
${ }^{n}$ : Number of properties, $D E_{z o}$ : Distance between points and center of palm, ${ }^{x_{z i}}$ : The coordinates of the ${ }^{i}$ property for ${ }^{Z}$ (points ), ${ }^{x_{o i}}$ : The coordinates of the ${ }^{i}$ property for ${ }^{o}$ (where ${ }^{o}$ : center point of palm)
Slop $=\frac{y z-y o}{x z-x o}$
Where:
 center value point of palm, ${ }^{x_{o}}$ : the ${ }^{X_{\text {- axis of }}}$ center value point of palm.
$x_{o}=\frac{\sum x_{o i} A_{i}}{\sum A_{i}}, \quad y_{o}=\frac{\sum y_{o i} A_{i}}{\sum A_{i}}$
Where:
$\mathrm{x}_{\mathrm{o}}$ : the ${ }^{\mathrm{X}}$ - axis of center value point of palm, ${ }^{\mathrm{Y}_{\mathrm{o}}}$ : the ${ }^{\mathrm{y}_{-}}$axis of center value point of palm, $\mathrm{X}_{\text {oii }}$ : The distance at which the center of the shape moves away from the junction point of the axes on the axis ( ${ }^{\mathrm{X}}$, ${ }^{\mathrm{Y}}$ oi: The distance at which the center of the shape moves away from the junction point of the axes on the axis $\left({ }^{\mathrm{y}}\right)$, $\mathrm{A}_{\mathrm{i}}$ : Area the shape.
$A=\frac{1}{2} \sum_{i=0}^{n-1}\left(x_{i} \times y_{i+1}\right)-\left(x_{i+1} \times y_{i}\right)$
n : Number of points, $\mathrm{X}_{\mathrm{i}}{ }^{\text {E }} \mathrm{x}$ - axis coordinates points, ${ }_{\mathrm{i}}{ }^{\text { }} \mathrm{y}$ axis coordinates points.
Per $=\sum_{i=0}^{n-1} x_{i}$
${ }^{n}$ : Number of ribs, ${ }^{\mathrm{x}}$ : length of the rib.
This features can be extracted by using algorithm.3.

## Algorithm 3

Input: binary image.
Output: features vector.

1. Calculate center point of palm as in equation (5).
2. Calculate the eight-features of distance by using equation (3), then evaluate the length of the palm and divide the distance by the length.
3. Calculate the eight-features of slop from center of palm for eight-points as according to equation (4).
4. Calculate area of hand as according to equation (6).
5. Calculate Perimeter of hand as according to equation (7).
6. Calculate the feature vector for all numbers types ( 40 types) by find the average of features for the same type numbers from different images of the same number.
7. End

In testing stage the features will be compare with stored features where the input image will be classifying into 40 type of numbers and comparing with the feature vector with the 244 vectors stored in the training stage, calculated the distance in three methods; Standardized Euclidean distance by using equation (8), Euclidean distance and correlation by using equation (9).
${ }^{\prime}$ Dst $=\sqrt{\sum_{i=1}^{n} \frac{\left(x_{i}-y_{i}\right)^{2}}{\sqrt{\frac{1}{(n-1)} \sum_{j=1}^{n}\left(x_{j}-\bar{x}\right)^{2}+\left(y_{j}-\bar{x}\right)^{2}}}}$
Where:
$x_{i}$ is the $i^{\text {th }}$ valuse of first vector value, $y_{i}$ is the $i^{\text {th }}$ valuse of second vector value, $n$ : is the number of elements in vector.,
$\bar{x}$ : is the mean value of first and second vector.
$R 1=\frac{\sum_{i}\left(x_{i}-x_{m}\right)\left(y_{i}-y_{m}\right)}{\sqrt{\sum_{i}\left(x_{i}-x_{m}\right)^{2}} \sqrt{\sum_{i}\left(y_{i}-y_{m}\right)^{2}}}$
Where:
$x_{i}$ is the intensity of the $i^{t h}$ value in vector 1, $y_{i_{\text {is the }}}$ intensity of the $i^{t h}$ value in vector $2,{ }^{\text {th }}{ }_{m_{\text {is }}}$ the mean intensity of vector 1 , and my is the mean intensity of vector2.

## 4. Results

The proposed algorithm contains two stages; training stage using 244 images while the second stage (testing) there are 80 images used for testing represent four languages. There are 18 features for distance (D1, D2 ... D8), slop (S1, S2 ... S8), area (A1) and perimeter ( P 1 ) respectively, then calculate the average for each type of number this will repeat for 40 type of numbers ten numbers for each language numbers as shown in Table.1. Table. 2 shows the feature vector of the average image for all images in the database. The results of the five clustering algorithms; Bayesian, K-mean, K-mediod, C4.5, and ANN, for different numbers types (40 types) had high accuracy as shown in Table.3. and Figure. 5
In testing stage the last step is to convert the decision (a type of number in four languages) into corresponding voices of four lan-
guages such as five，بنج ，五 or the first writing the same alphabet then play the sound that represents that number．
Table 1：Features vector of four languages numbers Feature Geometry

| Feature Geometry |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Distance |  |  |  |  |  |  |  | Slope |  |  |  |  |  |  |  | A1 | P1 | Language |
| D1 | D2 | D3 | D4 | D5 | D6 | D7 | D8 | S1 | S2 | S3 | S4 | S5 | S6 | S7 | S8 |  |  |  |
| $\stackrel{N}{\infty}$ | $\underset{\underset{0}{\infty}}{\substack{0}}$ | $\underset{\underset{\sim}{0}}{\stackrel{H}{0}}$ | $\stackrel{7}{ \pm}$ | $\stackrel{\sim}{2}$ | $\frac{n}{3}$ | $$ | $\begin{aligned} & \text { m} \\ & \underset{o}{0} \end{aligned}$ | $\begin{aligned} & \text { N} \\ & \text { N} \\ & \text { O} \end{aligned}$ | $\begin{aligned} & \text { N} \\ & \underset{\sim}{4} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { Q} \\ & \stackrel{\rightharpoonup}{7} \end{aligned}$ | $\stackrel{\ominus}{寸}$ | $\begin{aligned} & \circ \\ & \stackrel{0}{\circ} \\ & \stackrel{\circ}{0} \end{aligned}$ | $\stackrel{\underset{\infty}{\infty}}{\underset{\sim}{0}}$ | $\underset{\sim}{\underset{\sim}{\mathrm{N}}}$ |  | $\stackrel{\infty}{\underset{\sim}{n}}$ | $\stackrel{n}{n}$ | \％ |
| $\begin{aligned} & \text { J } \\ & \substack{\infty\\ } \end{aligned}$ | $\underset{\sim}{n}$ | $\stackrel{\rightharpoonup}{\infty}$ | $\stackrel{ \pm}{\infty}$ | ते | N | 4 $\stackrel{n}{0}$ 0 | $\begin{gathered} \text { N} \\ \substack{\infty \\ 0} \end{gathered}$ | $\begin{gathered} \underset{\sim}{*} \\ \stackrel{\sim}{*} \\ 0 \end{gathered}$ | $\begin{aligned} & 2 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\begin{gathered} \underset{\text { G}}{\substack{2}} \\ \hdashline \\ \hline \end{gathered}$ | $\begin{aligned} & \text { ñ } \\ & \stackrel{0}{n} \\ & \end{aligned}$ | $\begin{aligned} & \frac{2}{8} \\ & \frac{0}{0} \end{aligned}$ | $\begin{aligned} & \circ \\ & \hline 0 . \\ & \hline 0 . \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\sim} \\ & \underset{\sim}{2} \end{aligned}$ | $$ | $\underset{\underset{\sim}{\infty}}{\stackrel{\infty}{\infty}}$ | N N 0 | \％ |
| $\stackrel{\stackrel{N}{3}}{\substack{0}}$ | $\stackrel{\square}{3}$ | $\frac{2}{6}$ | $\frac{5}{8}$ | $\stackrel{\sim}{\infty}$ | $\overline{0}$ <br> 0 | $\begin{aligned} & \circ \\ & \stackrel{\circ}{0} \\ & \stackrel{0}{\circ} \end{aligned}$ | $\begin{aligned} & n \\ & \frac{n}{0} \end{aligned}$ | $\stackrel{0}{N}$ | $\begin{aligned} & \text { 응 } \\ & \text { on } \end{aligned}$ | $\begin{aligned} & \infty \\ & \stackrel{\infty}{\circ} \\ & \stackrel{N}{+} \\ & \hline \end{aligned}$ |  | $\stackrel{\sim}{2}$ | $\begin{aligned} & \text { N} \\ & \text { Ǹ } \\ & \text { Ǹ } \end{aligned}$ | $\begin{gathered} \text { N} \\ \underset{\sim}{c} \end{gathered}$ | $\underset{\substack{\text { N} \\ \hline}}{ }$ | $\stackrel{\infty}{\stackrel{\infty}{\infty}}$ | ¹ $\substack{6 \\ 0}$ | ． |
| $\begin{aligned} & \text { N゙ } \\ & \text { N゙ } \end{aligned}$ |  | $\stackrel{n}{\infty}$ |  | त N | त तु | $\frac{0}{6}$ | $\begin{gathered} \text { N్ల } \\ \text { N゙ } \end{gathered}$ | $\begin{aligned} & \text { to } \\ & \text { N} \\ & \text { N} \end{aligned}$ | $\stackrel{N}{\text { N }}$ | $\xrightarrow[\substack{\text { Ǹ } \\ \text { N} \\ \cdots}]{ }$ | $\begin{aligned} & \text { O} \\ & \stackrel{\rightharpoonup}{\top} \end{aligned}$ | $\stackrel{\circ}{\infty}$ |  | $\begin{aligned} & N \\ & \underset{\sim}{n} \\ & 0 \end{aligned}$ | ¢ | \％ | $\stackrel{\infty}{\circ}$ | 5 $=00$ （1） |

Table 2：Features vector for average of number six in four language

| Feature Geometry |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Distance |  |  |  |  |  |  |  | Slope |  |  |  |  |  |  |  | A1 | P1 | Language |
| D1 | D2 | D3 | D4 | D5 | D6 | D7 | D8 | S1 | S2 | S3 | S4 | S5 | S6 | S7 | S8 |  |  |  |
| $\stackrel{\sim}{\infty}$ | $\underset{\underset{\infty}{\infty}}{\substack{\infty}}$ | $\stackrel{\underset{\sim}{m}}{\substack{0}}$ | $\stackrel{\rightharpoonup}{\square}$ | $\stackrel{2}{7}$ | $\frac{n}{3}$ | $\underset{\substack{\text { N } \\ \text { N } \\ \hline}}{\text { + }}$ | $\begin{gathered} \text { m } \\ \text { N} \\ \hline 1 \end{gathered}$ |  | $\begin{aligned} & \stackrel{0}{+} \\ & \underset{\sim}{+} \\ & \stackrel{1}{2} \end{aligned}$ | $\begin{aligned} & \circ \\ & \stackrel{\circ}{\circ} \\ & \underset{-}{7} \end{aligned}$ | $\stackrel{R}{7}$ | $$ | $\stackrel{\infty}{\infty}$ | $\underset{\substack{\text { I } \\ ?}}{\text { n }}$ |  | $\stackrel{\infty}{\stackrel{\infty}{\pi}}$ | n | 0 0 \＃ |
| N $\substack{0 \\ 0}$ | $\begin{aligned} & 2 \\ & \frac{2}{3} \end{aligned}$ | $\frac{2}{6}$ | $\stackrel{3}{8}$ | $\stackrel{\infty}{\stackrel{\infty}{0}}$ | $\begin{aligned} & \stackrel{\infty}{0} \\ & \stackrel{i}{0} \end{aligned}$ | $\begin{aligned} & \circ \\ & \stackrel{\circ}{\circ} \\ & 0 \\ & \hline \end{aligned}$ | $\begin{aligned} & n \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\frac{0}{\widehat{0}}$ | $\begin{aligned} & \hat{o} \\ & \text { B } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \infty \\ & 0 \\ & \underset{\sim}{0} \\ & \underset{\sim}{n} \end{aligned}$ | $\begin{gathered} \underset{\sim}{N} \\ \stackrel{N}{7} \end{gathered}$ | $\stackrel{\text { N }}{\substack{2 \\ \vdots}}$ | $$ |  | $\stackrel{\text { N}}{\substack{\text { on }}}$ | $\stackrel{\infty}{\stackrel{\infty}{\circ}}$ | \％ $\substack{\text { ¢ } \\ 0 \\ 0}$ | \％ |
| $\begin{aligned} & \text { d } \\ & \text { N } \\ & \text { N} \end{aligned}$ | N Ṅ | $\stackrel{\bar{\infty}}{\stackrel{\square}{0}}$ | $\frac{ \pm}{\frac{8}{0}}$ | ते | $\frac{\tilde{y}}{\underset{O}{\mathrm{O}}}$ | $\begin{gathered} \underset{\sim}{3} \\ \stackrel{\sim}{0} \end{gathered}$ |  | $\underset{\substack{\underset{\sim}{*} \\ \multirow{2}{*}{\hline}\\ \hline}}{ }$ | $\begin{aligned} & 2 \\ & 0 \\ & 0 \\ & 0 \end{aligned}$ | $\stackrel{\Im}{\Im}$ | $\begin{aligned} & \text { n} \\ & \text { ion } \\ & \cdots \\ & \end{aligned}$ | $\frac{\hat{8}}{3}$ | $\begin{aligned} & \circ \\ & \hline 0 \\ & \hline 0 \\ & \hline 0 \end{aligned}$ | $\begin{aligned} & \underset{\sim}{\mathrm{F}} \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { N } \\ & \stackrel{y}{0} \\ & 0 \end{aligned}$ | $\stackrel{\infty}{\underset{\sim}{\infty}}$ | N $\substack{\infty \\ 0}$ | 第 |
| $\begin{aligned} & \text { N} \\ & \underset{O}{4} \end{aligned}$ |  | $\stackrel{\sim}{\infty}$ |  | $\begin{gathered} \underset{\sim}{J} \\ 0 \end{gathered}$ | $\begin{aligned} & \text { ®్ర } \\ & \text { ci } \end{aligned}$ | $\frac{8}{2}$ | $\begin{gathered} \text { N゙ } \\ \text { N゙ } \end{gathered}$ | $\begin{aligned} & \text { tion } \\ & \text { ci } \end{aligned}$ | $\stackrel{N}{N}$ | $\xrightarrow[\text { Ǹ }]{\substack{\text { Ǹ } \\ \vdots}}$ | ® $\stackrel{\text { ¢ }}{\sim}$ $\sim$ | $\stackrel{\infty}{\infty}$ | ぶ | $\begin{aligned} & \mathrm{N} \\ & \underset{\infty}{\infty} \\ & \stackrel{0}{2} \end{aligned}$ | $\begin{aligned} & \underset{\sim}{8} \\ & \substack{0 \\ 0} \end{aligned}$ | \％ | $\stackrel{\infty}{\stackrel{\infty}{\circ}}$ | 5 00 － |

Table 4：the accuracies of the four algorithms
Table 4：the accuracies of the four algorithms

| Number | No image | Bayesian | C4．5 | K－mean | K－mediod | ANN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 244 | $100 \%$ | $100 \%$ | $100 \%$ | $100 \%$ | $95 \%$ |

As shown in Table ．4，the Bayesian，C4．5，K－mean and K－mediod algorithm achieves the highest recognition accuracy100\％，while ANN gave low than them $95 \%$ ．


Figure 5：accuracy rate between five algorithms

## 5．Conclusion

In this paper，we have designed an algorithm for recognition four languages number based on clustering methods．The experiments
show that the geometric features are best features than others fea－ tures；shape，texture，colored．．．etc．These features（geometric features）achieved higher accuracy than the others．Classification algorithms used in our proposed algorithm such as Bayesian，K－
mean, K-medoid, C4.5, and ANN shows that Bayesian, K-mean, K-medoid, C4.5.5 algorithms are the best one in clustering or classifying with percentage of $100 \%$, it is better than using other classification method such as GLCM which used in texture features and DWT which used with statistical features. In the testing stage, we found that the three methods; modified Standardized Euclidean distance, Euclidean distance and Correlation are the best metrics for recognition the 40 numbers.

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