

Some Factors Affecting on Magnetic Characteristic Quantities and T_c Curie Phase Transition Temperature of the Ni Nanoparticles by the Classical Heisenberg Model

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Abstract

This paper investigates the effect of particle size $D = 4.51\text{nm}, 5.03\text{nm}, 5.42\text{nm}, 5.91\text{nm}$, rate of heat $4.10^{12}\text{K/s}, 4.10^{13}\text{K/s}, 4.10^{14}\text{K/s}$ on magnetic characteristic quantities: Magnetization M , specific heat C_v , energy E , magnetic susceptibility χ and T_c Curie phase transition temperature by classical Heisenberg model. The results show when increasing D particle size then T_c Curie transition temperature increases and when increasing rate of heat then T_c decreasing. In addition, there is the influence of D size and heating rate on magnetic characteristic quantities.

Keywords: influence, particle size, rate of heat, T_c Curie transition temperature, classical Heisenberg model.

1. Introduction

Now, Ni nanomaterials are being used in the science, technology and biomedical. Optical catalysts [1], [2], photovoltaics [11], solar cells [3], [4]. .. To create the Ni nanoparticles, there are many methods. Chemical methods [5], [6], [7], physical methods [8], [9] ... and molecular dynamics simulation methods [30] and Monte-Carlo method [31]. The results showed, T_m phase transition temperature always proportional with $N^{-1/3}$ atoms number [10], [11], [12], [13], [14], [15], T_g crystallization temperature of the nanowires always inversely proportional with D size [11] and T_c Curie phase temperature be determined by semi-empirical formula give results smaller than 631K [16]. For size $D = 24\text{nm}, 50\text{nm}, 96\text{nm}, 165\text{nm}, 200\text{nm}$ then $T_c = 593\text{K}, 612\text{K}, 622\text{K}, 626\text{K}, 627\text{K}$ and when D decreases then T_c decreases [17], [18], [19], [20], [21], [22], [23], [24], [25], [26], [27], [28], [29]. In addition, there is also the effect of Ni nanoparticle size [49] and thin film thickness [50] on T_c Curie transition temperature. Recently, investigated the effect of rate of heat, atomic number, temperature, and heating time on structure of Ni nanoparticles by Molecular Dynamics method with Sutton-Chen interaction, boundary conditions freedom [30] and characteristic quantities magnetic of Fe nanoparticles [31]. The results show, has influence of D particle size on structure and magnetism. When increasing atomic number N lead to D particle size increases proportional with $N^{-1/3}$ and energy increases proportional with N^{-1} [30] and appearance of BCC structure is interesting and controversial. With calculations based on analysis: Structural [45], [47] link angle analysis [46], link analysis [48] ... will solve this problem, T_c Curie phase temperature increased [31]. In the article, influence of D particle size, rate of heat on magnetic characteristic quantities and T_c Curie phase transition temperature of Ni nanoparticles.

2. Calculation Method

The study Ni nanoparticle with density ρ and nanoparticle size

$$\text{evaluated by } D = 2 \left(\frac{3N}{4\pi\rho} \right)^{1/3} \quad (1)$$

with $\rho = 7.72 \text{ g.cm}^{-3}$. Inside N, V are atoms numbers total and volume of particle. Ni nanoparticles generated by molecular dynamics method with embedded interaction Sutton-Chen and free boundary condition [30]. The thermal processes follow law of Nosé el [43] and Hoover el [44]. To determine magnetic characteristic properties, considered each atom of Ni nanoparticle is a spin S_i , magnitude value of each spin is $|S_i| = 1$. Place Ni nanoparticles into classical Heisenberg model [32], [33], [34] with Hamilton function has form:

$$H = - \sum_{i,j \in R(i)} J_{ij}(\mathbf{r}_{ij})(S_i \times S_j) \quad (2)$$

$$\text{In it } J_{ij}(\mathbf{r}_{ij}) = J_0 \left(1 - \frac{|\mathbf{r}_{ij}|}{r_c} \right)^3 \quad (3)$$

With J_0 is interaction energy between two nearest spins, $\mathbf{r}_{ij} = |\mathbf{r}_i - \mathbf{r}_j|$ is shortest distance between two spins S_i, S_j and J_{ij} is interaction energy between spins S_i, S_j and $r_c = 3.35\text{\AA}$ is radius breaker. After that determining magnetic characteristics of nanoparticles Ni as:

$$\langle E \rangle = \frac{1}{N} \langle H \rangle, \langle M \rangle = \frac{1}{N} \left\langle \left(\sum_i S_i \right) \right\rangle,$$

$$\langle C_v \rangle = N \frac{\langle E^2 \rangle - \langle E \rangle^2}{(k_B T)^2}, \langle \chi \rangle = N \frac{\langle M^2 \rangle - \langle M \rangle^2}{k_B T} \quad (4)$$

and T_c Curie phase transition temperature.

Inside, magnetic characteristic quantities has related to J_0 interaction energy which is currently unknown by theory model well as in empirical. used Moten-Carlo method, combined with error method of physical quantity measurement to determine J_0 by:

First, determining average value of $\bar{T}_c = \frac{1}{N} \sum_{i=1}^N T_c$ and

absolute error $\Delta T_c = |T_c - \bar{T}_c|$ of Ni_{4000} nanoparticles with $D = 4.51nm$ according $J_0 = 0.4; 0.5; 0.6; 0.61; 0.63; 0.65; 0.67; 0.69; 0.7; 0.8$ and comparing obtained results T_c with results of semi-

empirical formula T_{es} (5) and then selecting J_0 with minimum ΔT_c absolute error.

$$T_{es}(D) = T_{c0} \exp\left(-\frac{2S_{vib}}{3R} \frac{1}{D/6h-1}\right) \quad (5)$$

With $S_b \approx S_m = 10, 12 J/mol.K$; $h = 0, 2492nm$; $T_{c0} = 631K$; $R = 8, 314 J/mol.K$ [35], [36], [37] have T_{es} of Ni nanomaterials. All of the nanoparticles were done with sufficient time to reduce statistical errors. Recovery time is 10^6 MC steps/spin and the average statistical time is 2.10^6 MC steps/spin.

3. Results and Discussion

3.1. Effect of J_0 Exchange Energy

To determine T_c Curie phase transition temperature of Ni_{4000} nanoparticle [30] with different J_0 exchange energy values, resulting Table 1, Figureure. 1

Table 1 Relationship between T_c Curie phase transition temperature with J_0 exchange energy of Ni_{4000} nanoparticles

J_0	$T_c(K)$	$\bar{T}_c (K)$	$\Delta T_c = T_c - \bar{T}_c (K)$
$J_0 = 0.4$	271.6	403.3	131.7
$J_0 = 0.5$	339.5		63.8
$J_0 = 0.6$	400.6		2.71
$J_0 = 0.7$	468.6		65.3
$J_0 = 0.8$	536.4		133.1

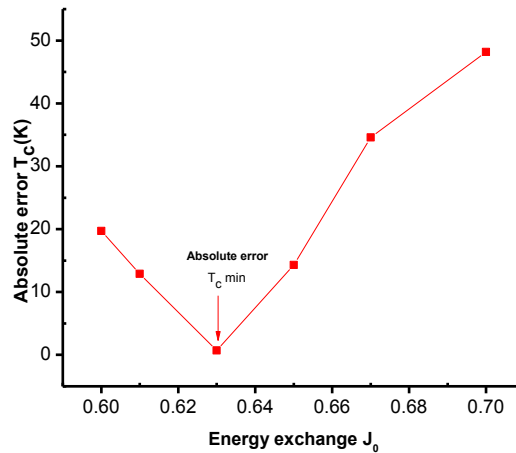


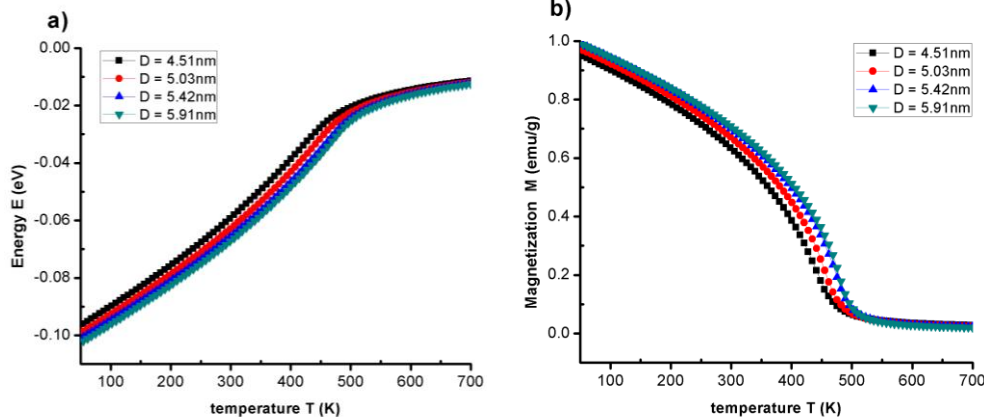
Figure 1 The relationship between the absolute error of T_c curie phase transition temperature with J_0 exchange energy values differently.

The results show, T_c Curie phase transition temperature has average value $\bar{T}_c = 403.3K$ (table 1) and in range $J_0 = (0.6; 0.7)$.

The detailed result shows $J_0 = 0.63$ has smallest absolute error (Figureure 1). So, choose $J_0 = 0.63$, with neighborhood radius $r_c =$

3.35\AA to study. This is method very useful for theory studies, empirical to determine J_0 values for a variety of materials.

3.2. Effect of D Particle Size



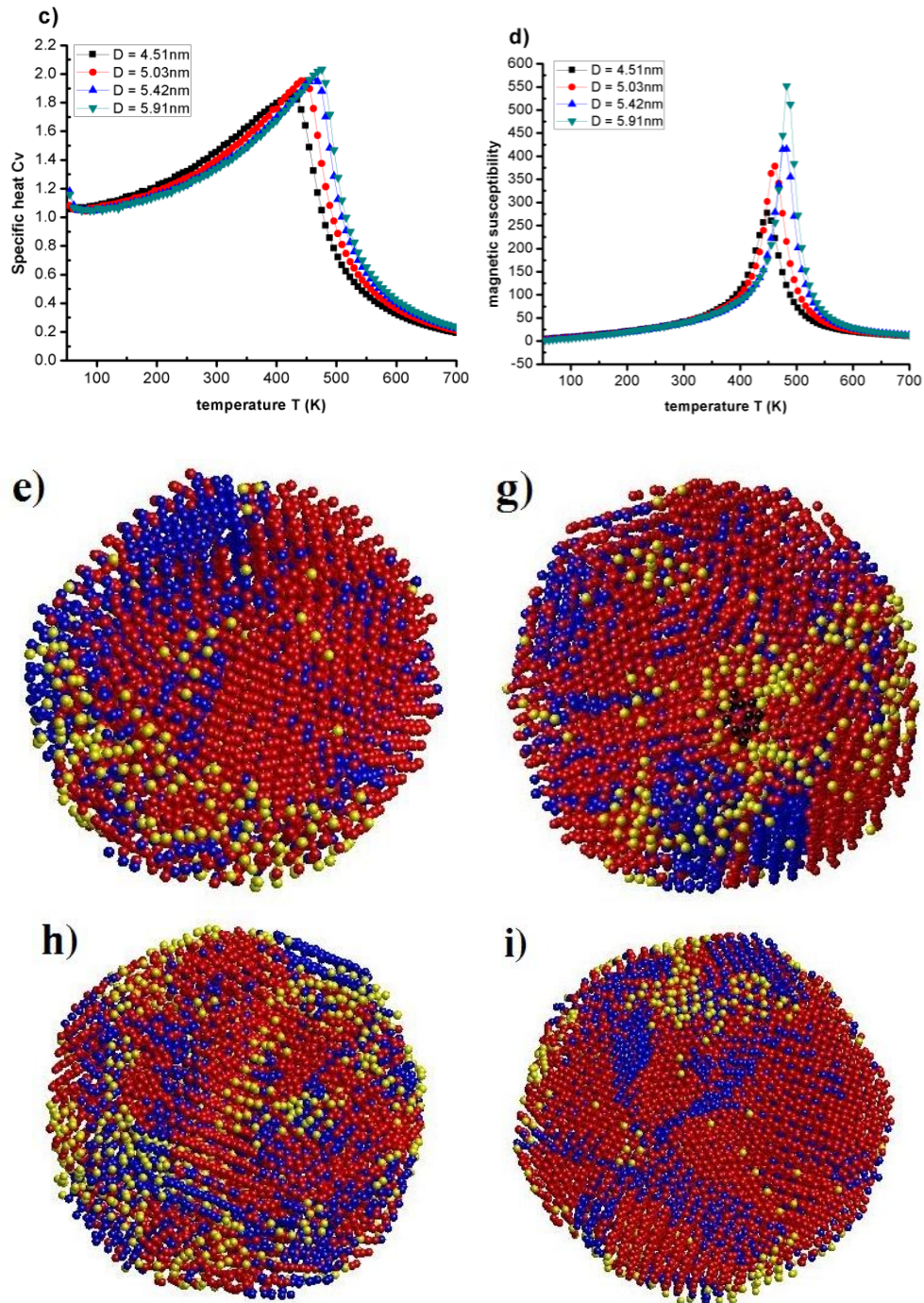


Figure 2. E Energy (Fig. a), M magnetization (Fig. b), C_v specific heat (Fig. c), χ magnetic susceptibility (Fig. d) with D different nanoparticle size: D = 4.51nm (Fig. e), D = 5.03nm (Fig. g), D = 5.42nm (Fig. h) and D = 5.91nm (Fig. i). Inside, atoms illustrated by Red colored for FCC structure, blue for HCP structure, black for BCC structure, yellow for Amor structure.

The results show, the have influence of D on E, M, C_v , χ . When D increases from D = 4.51nm to 5.91nm then E decreases from -0.0972eV to -0.1003eV (Fig. 2a); M decreases from 1 to 0 and curvature descending (Fig. 2b); C_v reached extreme value at T_c , height of peak increased from 1.79257 to 2.0118 (Fig. 2c); height of peak increased from 276.59 to 550.83 (Fig. 2d). The displays for each T values correspond to a value M, C_v , E, in particular. The display values do not include errors because error value at point each has less than size of display value. When $T < T_c$ then the curvature of the magnetization curve M increases when increasing D (Fig. 2b), decreasing when $T > T_c$ and this is the basis for existence ferromagnetic phase transition on Ni nanoparticles.

In addition, the results of Fig. 2c, Fig. 2d show that extreme values of C_v and χ increase when D increases and confirmed that

T_c Curie phase transition temperature of Ni nanoparticles is phase transition temperature of type 1. To the observe structure of Ni nanoparticles, used the visualization method (Fig. 2e-2i). The results show, nanoparticles are made up of FCC, HCP, BCC, Amor structures and assert there is no messy arrangement of Ni atoms but instead is an arrangement of atoms according to the definite structure. In Ni_{5324} nanoparticle has the appearance of BCC structure, explained in the article [30]. When increase N atoms number leading to D increase and E decreases it shows has the influence of D nanoparticle size on Ni nanoparticle structure. To confirm the accuracy of results, compared results T_c simulation with results of semi-empirical formula $T_{es}(5)$ [28], [29], [36], results in Table 2, Figure 3.

Table 2. Comparison T_c Curie phase transition temperature of simulation method and T_{es} Curie phase transition temperature of semi-empirical with D different nanoparticle size.

N Number (atoms)	4000	5324	6912	8788
D Size (nm)	4.51	5.03	5.42	5.91
T_c (K) (simulation)	421 ± 3	448 ± 2	461 ± 4	475 ± 6
T_{es} (K) (semi-experimental formula) [28], [29], [36]	422	448	463	479

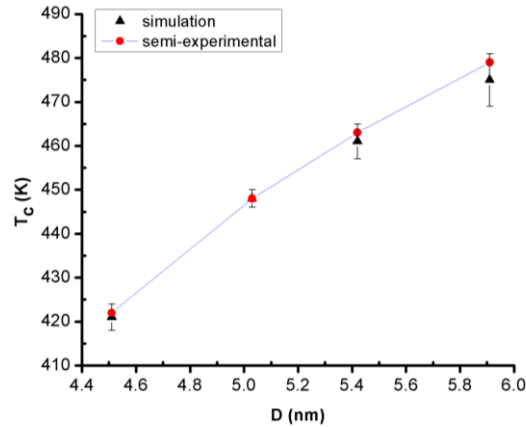


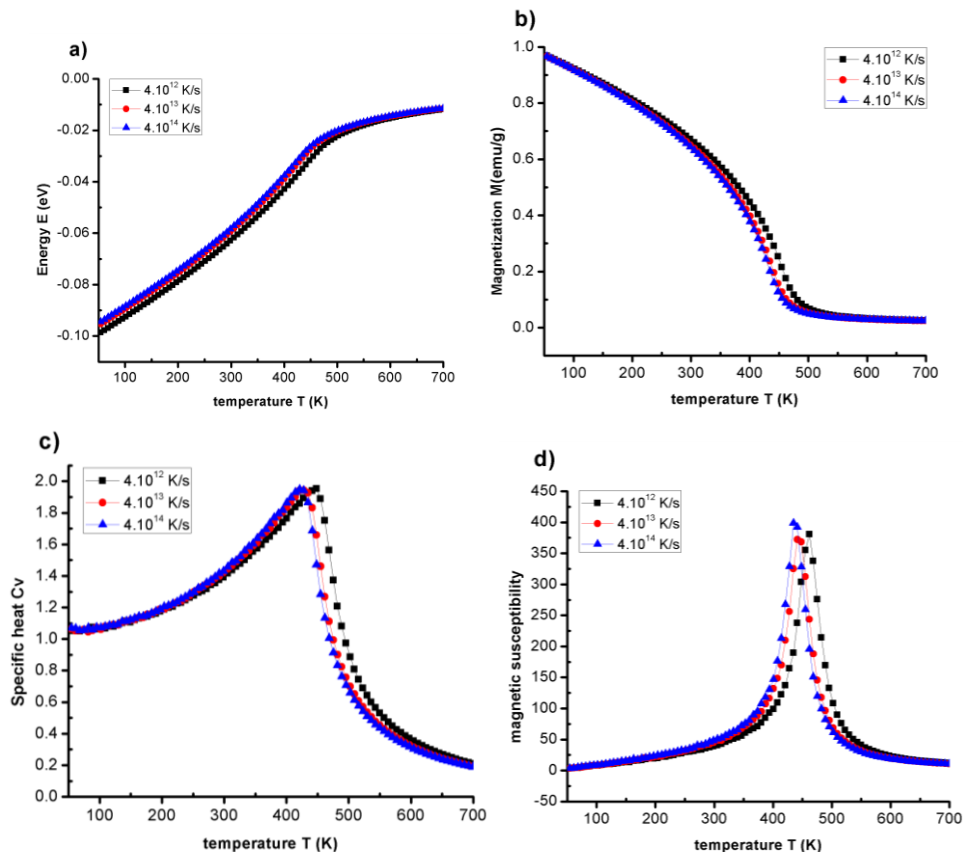
Figure 3. The relationship between T_c Curie phase transition temperature of simulation method and T_{es} Curie phase transition temperature results of semi-empirical formula with D nanoparticles sizes differently.

The results show, with each value of D will have T_c value, T_{es} respectively. To evaluate error at each value T_c and T_{es} use the interpolation method. These results showed, table 2 including T_c value respectively, error value at each point and T_{es} is determined by semi-empirical formula (5) to the comparison. Here determined the relationship between T_c and T_{es} : $T_{es} = T_c \pm (2 \text{ or } 6) \text{ K}$ with D increased from 4.51 nm to 5.91 nm. After comparing results between T_c and T_{es} [28], [29], [36] (Fig. 3) show results has duplication. The simulated results show that it is not only consistent with results of semi-empirical formula but also good fit with simulation results of bulk material and thin films [29], [38],

[39], [41], [42], [49], [50] the value obtained within allowable limit and confirmed by influence of D on magnetic characteristic quantities and T_c .

3.3 Effect of Heating Rate

To study magnetic characteristics and T_c Curie phase transition temperature at different structural states corresponding with different heating rates results in Figure 4



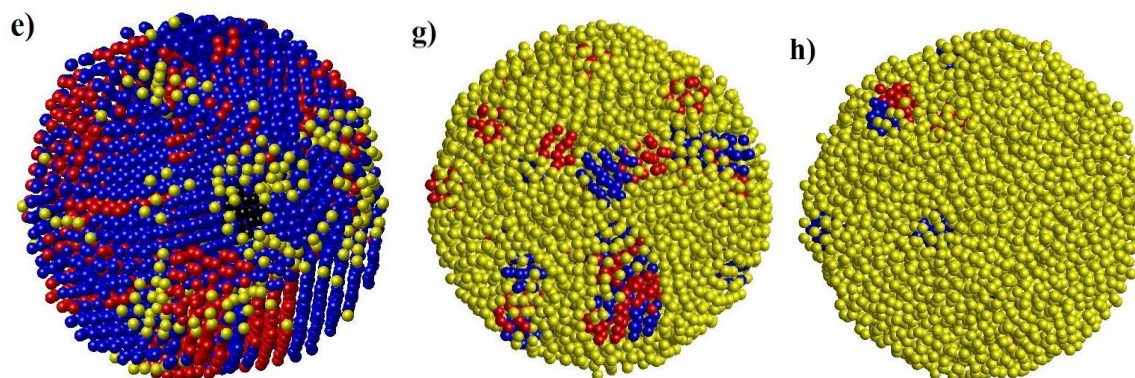


Figure 4 Magnetic characteristics of Ni₅₃₂₄ nanoparticles: Energy (Fig. a), magnetization (Fig. b), specific heat (Fig. c), magnetic susceptibility (Fig. d) with different heating rates 4.10¹³K/s (Fig. e), 4.10¹³K/s (Fig. g), 4.10¹⁴K/s (Fig. h) at temperature of T = 300K.

The results show, when increased rates of heating from 4.10¹²K/s to 4.10¹⁴K/s then energy increased (Fig. 4a), magnetization decreases (Fig. 4b), specific heat is constant (Fig. 4c) while magnetic susceptibility change negligible (Fig. 4d). When heating rate increases lead to T_c Curie phase transition temperatures decreases it shows Ni nanoparticles have moved on the amorphous state. Results structural change from crystalline state to the amorphous state leading to energy increased. The structural shape results (Fig. 4e-4h) shown HCP, FCC structural unit number decrease, and Amor increase is 93.98%. These results are consistent with results shown in Figure 4a-4d and very useful for studying structure and magnetism of Ni nanoparticles.

4. Conclusion

Study on effect of particle size, the heating rate on magnetic characteristic and Curie T_c phase transition temperature of Ni nanoparticles, results obtained: Successful determination of nanoparticle exchange energy is 0.63. When nanoparticle size increased lead to T_c Curie phase transition temperature increased, results were consistent with article [28], [29], [36]. When heating rate increases lead to structure changes from crystalline state to the amorphous state resulting T_c decrease. This is due to the structural change from crystalline state to the amorphous state leading to energy increased. The simulated results show it is not only consistent with the results of the semi-empirical formula but also consistent with results of bulk material and thin films [29], [38], [39], [41], [42], [49], [50].

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