

Comparison of Transmission Loss Allocation by Proportional Sharing Principle Method and Aumann Shapley Method

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Abstract

In the current scenario of the electricity market in the world the cost allocation became the thematic part and the essential usage to individual distributor and to the consumer. Allocation is nothing but a share of anything that has been shared in the equal amount to the assigned terms of the quantity. Here in the power sector, losses and the respective costs have been shared among the generators and the loads. To achieve the linear nature and invariant characteristics, allocation of losses is done. To such allocation of losses there are many methods, popular methods of them named, Proportional Sharing Principle Method and Aumann-Shapley Method are compared in this paper based on loss and cost allocation, and results are verified through Mat lab platform.

Keywords: Loss Allocation; Generator; Loads; Proportional Sharing Principle Method(PSP Method); Aumann Shapley Method (AS Method); Transmission line system.

1. Introduction

Transmission loss distribution is critical in modernized power advertise. Since generators and power customers are altogether associated with the power framework, varieties in any of the patrons can have a momentous impacts on others making it trying to research the cost, each power network is in charge of it. It is hard to accomplish a proficient transmission loss designation in every one of their parts of the section. To analyze and allocate such losses through the various methods with their methodologies. Allocation is nothing but a share of anything that has been shared in the equal amount to the assigned terms of the quantity. Throughout a close to several methods that had taken place to allocate losses their main and thematic principle is that to share the loss equally to the respective generators and loads.

Electrical power transmission system:

Amid development of producing station number of variables are to be considered from the financial perspective. These all components may not be easily open at stack focus; subsequently making stations are not customarily organized nearer to stack focus. Load focus is the place which consumes most noteworthy power. Hereafter there must be a couple of means by which we can transmit the made vitality to the store stack. Electrical transmission structure is the techniques for transmitting power from making station to different load centers.

What is loss allocation? And why it is required?

It is sureness that the unit of electric essentialness created by Power Station does not organize with the units dispersed to the shoppers. Some level of the units is lost in the movement organize. This complexity in the made and scattered units is known as

Transmission and Distribution loss Transmission. What's more, Distribution losses is the whole that is not paid for by buyers.

What happens when loss allocation is done?

To align such losses among the transmission line system, different types of methods are used to allocate. Allocation should be:

1. Straightforward and in view of genuine information of the system;
2. Precisely intended to maintain a strategic distance from segregation between clients;
3. Ready to recoup the aggregate sum of the losses;
4. Predictable with the guidelines of competitive power markets.
5. There will be a literal quantity of sharing in the loss and cost allocation that it carries away.

Advantages of loss allocation:

In rebuilt power systems all of system task costs must be allotted amongst purchasers and generators through correct direction to avoid unfairness. Both of generators and purchasers should pay arrange loss cost in view of together utilizing system structure. In view of nonlinear connection between system loss and generation and loads, correct allocating system losses amongst generators and burdens is troublesome. The majority of detailed strategies for loss distribution is for transmission arrange. The allotment of the system losses to distributors and consumers is a testing issue for the rebuilt power commerce.

If the loss allocation doesn't takes place then:

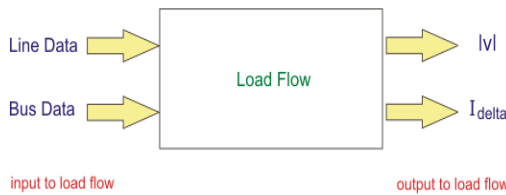
The system gets more occurrence of variance in the power that been consumed and so there will be a vast difference in the cost to such power unit value.

A nonlinear nature occurs with the system and so the disturbances occurs with the various power consumption. Hence to resolve all these losses within the system loss allocation is used to exhibit the equality in all aspects when losses occur. So to convey and to have equal conveyance in the cost and loss allocation throughout the system with the consumers, this phase has to be used.

As far the paper is aligned and contributed with the allocation and why it been required so? Now a challenging that takes place is allocation is done with the methodology of?

A load flow analysis is the theme part to have such allocation process:

Load stream examination is the most critical and fundamental way to deal with exploring issues in control framework working and arranging. In view of a predefined creating state and transmission arrange structure, stack stream examination unravels the relentless task state with hub voltages and branch control stream in the power framework. Load stream investigation can give an adjusted relentless task condition of the power framework, without thinking about framework transient procedures It is the numerical calculation required to decide the consistent state working qualities of a power network arrange from the given line information and transport information. The yield of the heap stream investigation is the voltage and stage point, genuine and responsive power, line losses and slack transport influence.



Load stream analysis insists of different methods to promote the analysis. To such here we have gone with the some of the techniques to the loss allocation. The methods that been considered are:

1. Newton Raphson method
2. Z Bus method
3. Gauss seidel method
4. Decoupled method
5. Fast decoupled method
6. Game theory
7. Y Bus method

The above methods that here we shown are used for various methods to have thematic part for the loss allocation process in the transmission system. Load flow analysis gives a great conclusion over the results which we assured to have in the transmission loss allocation and to some of the methods that we need are very useful to calculate the cost to such the losses allocation and so as a part we made it as the cost allocation to the extent. The methods and their methodologies with the thematic phase of the load flow analysis and the types that been discussed in this paper are as follows with their principles and their methodologies.

1. Proportional sharing principle method
2. Aumann Shapley method

Proportional Sharing Principle Method:

This technique explains with the levels of the electrical laws. To allocate the losses to singular generators and demands, the strategy relies upon unobtrusive rule, that the misfortunes related with a specific hub in influence stream organize which is relatively shared by every one of the ways going out from that hub accordingly fulfilling Kirchhoff's present law. This law is simply a mo-

ment to say that equal sharing of loss allocation is to be maintained such that the subsidy and negation should be so simple easy to handle the electrical scenario and so we will look to have great relation and the methodology with which we assigned here.

The use of the delayed consequences of a unified power stream in collection to the immediate PSP technique similar division standard make it workable for the dispersion of misfortunes to generators and buyers. This decide communicates that "the power stream achieving a vehicle from any electrical link parts among the lines exhausting force from the vehicle moderately to their looking at control streams," which is neither provable nor disprovable. Comparing sharing system, over electrical laws, require the suspicion of the relative sharing rule. Utilizing this rule, losses are allotted by direct strategies.

The losses distribution ought to have some attractive properties as beneath:

1. To be reliable with the consequences of energy stream.
2. To rely upon the measure of vitality either created expended.
3. To be simple and transparent.
4. To give amend negligible signs to the system.

To dispense losses to demands, the technique depends on a basic guideline: losses related with each line whose stream enters a given transport are traded to the lines whose streams leave the flow (or demands in that transport) moderately to the floods of those lines (the surges of which leave the transport). It ought to be noticed that a deliberate use of this standard starts that all losses are dispensed to demands. Comparably, to dispense losses to generators, the strategy depends on a straightforward principle: losses related with each line whose flow leaves a given transport are exchanged to the lines whose streams enter the transport (or ages in that transport) relatively to the streams of those lines (whose streams enter the transport).

$$P_{i-j}(gross) = \left(\frac{P_{ij}}{P_i}\right) \sum [A_{u(i,k)}]^\wedge - 1 P_{GK} \text{ for } j \in \alpha_i^d \quad (1)$$

$\alpha_i^d = \text{set of Bulges provided from bulge } i$

$P_i = \text{Nodal power}$

$K = \text{Buses (generator bus)}$

$P_{GK} = \text{Creating power at } k$

$P_{ij} = \text{Branch flow (i=upstream, j=downstream)}$

$A_u = \text{Upstream distribution matrix}$

$$P_{i-j}^{(net)} = \left(\frac{P_{ij}}{P_i}\right) \sum [A_{d(i,k)}^{-1}] P_{DK} \text{ for } j \in \alpha_i \quad (2)$$

$K = \text{buses (load bus)}$

$P_{ij} = \text{Branch power flow}$

$\alpha_i^u = \text{set of nodes supplying node } i$

$A_d = \text{Downstream distribution matrix}$

Keeping in mind the end goal to relegate half of the losses to the generators and half to the demands, the last age and request per transport are figured as:

$$P'_{Gi} = (P_{i-j}^{net} + P_{Gi})/2 \quad (3)$$

$$P'_{Dj} = (P_{i-j}^{Gross} + P_{Dj})/2 \quad (4)$$

And to that the final stream losses allocated to each and every one generator and load is given by means of:

$$L'_{Gi} = P_{Gi} - P'_{Gi} \quad (5)$$

$$L'_{Di} = P_{Dj} - P'_{Dj} \quad (6)$$

Aumann Shapley Method:

This hypothesis is utilized for complex losses allocation among generators and burdens, in this specific submission, both the Shapley and Aumann-Shapley strategies prompt comparative equations for losses distribution. Be that as it may, not at all like the Shapley strategy, the Aumann-Shapley technique ensures isonomy concerning the measure of operators. Complex losses are distributed to generators and demands thinking about electric circuit laws and representing all truisms of the Aumann-Shapley hypothesis. The main thematic part of the proposed strategy take after:

- 1) It considers circuit laws and meanwhile has alluring qualities to the extent financial lucidness
- 2) It perceives and measures the individual responsibility of dynamic and receptive streams into dynamic and receptive power misfortunes.
- 3) It completely allocates the dynamic and responsive losses (full cost recuperation), because of the additional substance property of the Aumann Shapley strategy.
- 4) The losses are assigned to generators and demands assessing singular operators, notwithstanding when they are in a similar transport.

Game Theory:

This Theory is the formal examination of essential authority where a couple of players must settle on choices that perhaps impact the choice of various players. Along these lines, amusement hypothesis manages any issue in which every player's system relies upon what different players do. Amusement Theory takes a gander at the objective conduct when every chief's prosperity relies upon the choice of others and his own. It is expected that the judiciousness of all players is of normal learning. A player is said to be sane on the off chance that he looks to play in a way which expands his own particular result. Result is the installment got toward the finish of diversion. It is for the most part utilized in control frameworks to anticipate agreement because of market control i.e. demoralize intrigue's that could limit result. The diversion hypothesis philosophies can be utilized to recognize non-focused situations (from showcase co-facilitator perspective) and limit the dangers in value choices (from participant's point).

Game theory applied to loss allocation:

The issue of distribution is to decide the obligation of operators on behalf of individually administration offered or requested by them. They are for the most part capable to some degree for the extra expenses. For instance, in a basic two-transport network, with one age and one load, plainly the line stream is the eventual outcome of the power gave by the generator and asked for stack. One request rises: who is responsible for mishaps in the transmission line? The most recognized answer is that the two generators and demands are in charge of losses as they exist together in a commonly profitable collaboration. Without stack, there is no necessity for losses.

Losses in conduction line can be expressed as a task of generator streams that run over the line.

$$S_{line} = I_{line} * \overline{I_{line}} * Z_{line} \quad (1)$$

$$S_{line} = \frac{(I_1^G + \dots I_k^G + \dots I_n^G) \cdot (I_1^G + \dots I_k^G + \dots I_n^G)}{(I_1^G + \dots I_k^G + \dots I_n^G)} \cdot Z_{line} \quad (2)$$

$$S_{line} = \left((I_{Lr}^G + \dots I_{Kr}^G + \dots I_{Nr}^G)^2 + (I_{Li}^G + \dots I_{Ki}^G + \dots I_{Ni}^G)^2 \right) * Z_{line} \quad (3)$$

Losses in transmission lines can be communicated both in capacity of generator identical current sources as in capacity of load

proportional current sources. It is conceivable to have the branch misfortunes articulation as an element of load streams. Thinking about the heaps as the present sources, it is conceivable to have the branch misfortunes articulation as a component of load streams:

$$S_{line} = I_{line} * \overline{I_{line}} * Z_{line} \quad (4)$$

$$S_{line} = (I_1^C + \dots I_j^C + \dots I_M^C) \cdot \overline{(I_1^C + \dots I_j^C + \dots I_M^C)} \cdot Z_{line} \quad (5)$$

$$S_{line} = \left((I_{1r}^C + \dots I_{jr}^C + \dots I_{Mr}^C)^2 + (I_{1i}^C + \dots I_{ji}^C + \dots I_{Mi}^C)^2 \right) * Z_{line}$$

We here by having the game theory applied to transmission line and having same equality towards the generators and to the loads. We may give as such like to be as below, but by considering the Generators as half line losses and the loads as the other half line losses.

$$S_G = \frac{1}{2} S_{line} \& S_D = \frac{1}{2} S_{line}$$

Aumann shapley methodology:

Game Theory considers the vital circumstance and subsequently it yields harmony comes about with inner effectiveness. Aumann Shapley (AS) strategy is received in powerful circumstances and henceforth discovers great applications in blockage administration. Here cost distribution issue is dealt with as partitioning the cost of a mutually utilized office among every one of the members with the assistance of co-agent diversion hypothesis.

First, the client request at every hub (Di) is parceled to an expansive number, K, of little request amounts of equivalent size, given by:

$$\Delta D_i = \frac{D_i}{K} \forall i = 1, 2, \dots, n$$

For k=1 to K An arrangement of Unconstrained and Constrained Scheduling issues are illuminated utilizing DC OPF with nodal requests given by

$$D_i(k) = k * \Delta D_i$$

Then short-run peripheral blockage cost (SRMCC), (Pi), of providing a client situated at hub "I" is first figured as:

$$\Pi_i = \frac{\partial(\Delta F)}{\partial D_i} = \lambda_i^c - \lambda^u$$

Thus the AS congestion prices π are then computed as the average of the SRMCCs over the K cases solved, i.e:

$$\Pi_i = \frac{1}{K} \sum_{k=1}^K \Pi_i(k).$$

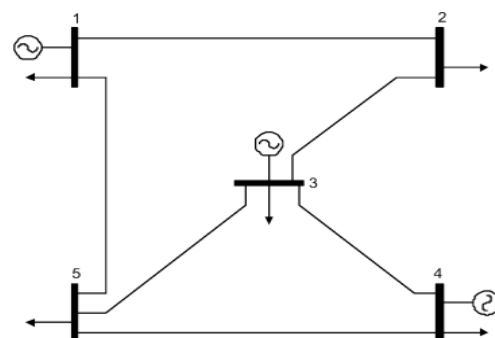


Figure1: Five Bus System.

So far in the paper there is a discussion about the methodologies and so and now with simplification throughout the results we will understand to know about how the methodology shows the analysis over the transmission loss system. In the above figure we are having the bus data and the line data and assigning as the 1,3 and 4 as the generators. Then 1,2,3,4 and 5 be the respective loads in the transmission system.

2. Results:

Table 1: Line data of the 5 Bus system.

S.No	From Bus	To Bus	R P. u	X P. u	B/2 P. u	X'Mer TAP(a)
1.	1	2	0.02	0.06	0.03	1.0
2.	1	5	0.08	0.24	0.25	1.0
3.	2	3	0.06	0.18	0.02	1.0
4.	3	5	0.04	0.12	0.015	1.0
5.	3	4	0.01	0.03	0.01	1.0
6.	4	5	0.08	0.24	0.025	1.0

In the above table it is been shown that the line data of the 5 bus system which here been assigned had taken and now move on to table consisting of bus data.

Table 2: Bus data of the 5 Bus system.

Bus	type	PGi	QGi	PLi	QLi
1	1	226.4	46.10	45	15
2	2	0.00	0.00	162.5	20
3	1	74.95	62.65	80	20
4	1	136.3	21.92	50	20
5	2	0.00	0.00	90	25

Here in the above table we are having the bus data of the 5 bus system which here been assigned had taken and now to the final results of the methodologies which we had taken as mentioned.

The section that discussed here is methodologies are awesomely described with the thematic way and now with the assigned platform mat lab we will gone through the coding and analyzed the loss allocation in the system through a great extent. We will get to know the results that the two themes here PSP method and the aumann shapley method gives the same performance in the loss allocation but to that such allocation there will be a minute changes in the occurrence of the loss that been came here in the consideration of the programming.

As with the consideration of the analysis and the methodology the aumann shapley method is well known with satisfaction of the 2 cases i).Constrained case ii).Unconstrained case. With a basic moto of the cases that been considered here is the unconstrained case. Now we will see the final result of the two methods that been compared is;

Table 3: Comparison of Methods.

S.No	From Bus	To Bus	PSP (Losses) (MW)	AS Method (losses) (MW)
1.	1	2	3.727	0.781
2.	1	5	0.864	0.864
3.	2	3	0.312	0.065
4.	3	5	0.409	0.409
5.	3	4	0.487	0.102
6.	4	5	0.439	0.439

In the above mentioned table we have gone through the results that we have got by the assigning of the data as we took and now hereby we had seen the such that the observation shows the both the methods are appropriate to such extent of the loss allocation and also to the cost allocation.

3. Conclusion

A comparison has been done with the respective busses and to such the losses allocated with their respective loads and the respective power flow. We here analyzed the results such that ob-

servation says that AS method shows to have clear and varied information in sharing the losses to the certain 5 bus system. And in the PSP method we have got good to allocate the losses and to have valid opinion on the sharing of losses. A committed conclusion to say is that in every method that which analyses to have loss allocation an equal sharing is done to their respective Generators and to the Loads in the transmission system. This comparison says us to acknowledge to have destruction in losses, so that to a great savage in the power system.

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